

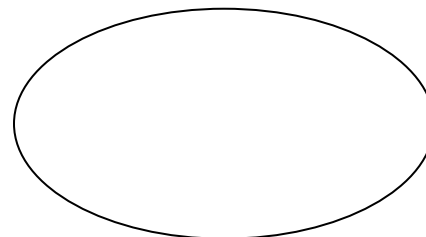
# KCSE 2023 TOP PREDICTION MASTER CYCLE 1

Name.....Adm No.....Class.....

School .....Candidate's Signature .....

## GRAND TOTAL

**MATHEMATICS**  
**PAPER 1**  
**TIME: 2 ½ HOURS**



**Mathematics**  
**Paper 1**  
**2½ hours**

### INSTRUCTIONS TO THE CANDIDATES

- This paper contains two sections; **Section I** and **Section II**.
- Answer all the questions in **section I** and only **five** questions from **Section II**.
- All workings and answers must be written on the question paper in the spaces provided below each question.
- Non programmable silent electronic calculators and KNEC Mathematical tables may be used **EXCEPT** where stated otherwise.
- Show all the steps in your calculations, giving your answers at each stage in the spaces below each question.

### FOR EXAMINER'S USE ONLY

#### Section 1

Question	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Total
Marks																	

#### Section 1I

Question	17	18	19	20	21	22	23	24	Total
Marks									

**SECTION I (50MKS)**

1. A rally car travelled for 2 hours 40 minutes at an average speed of 120km/h. The car consumes an average of 1 litre of fuel for every 4 kilometers. A litre of fuel costs Ksh.59. Calculate the amount of money spent on fuel. (3mks)
  
2. One interior angle of a polygon is equal to  $80^\circ$  and each of the other interior angles are  $128^\circ$ . Find the number of sides of the polygon. (3mks)
  
3. (a) Using a pair of compasses and a ruler only construct a triangle ABC and such that  $AB = 4\text{cm}$ ,  $BC = 6\text{cm}$  and  $\angle ABC = 135^\circ$ . (2mks)
  
- (b) Construct the height of triangle ABC in (a) above taking AB as the base, hence Calculate the area of triangle ABC. (2mks)

4. Solve the following inequalities and state the integral values (3mks)  
 $2x - 2 \leq 3x + 1 < x + 11$

5. Without using mathematical tables or calculators, **evaluate**  $\sqrt{\frac{1408 \times 0.594 \times 0.012}{6.05 \times 125}}$  leaving your answer as a simplified fraction (3mks)

6. Two similar solids have surface areas  $48\text{cm}^2$  and  $108\text{cm}^2$  respectively. Find the volume of the smaller solid if the bigger one has a volume of  $162\text{cm}^3$ . (3mks)

7. A triangle flower garden has an area of  $28\text{m}^2$ . Two of its edges are 14 metres and 8 metres. Find the angle between the two edges. (3mks)

8. A watch which loses a half a minute every hour. It was set to read the correct time at 0445hr on Monday. Determine in twelve hour system the time the watch will show on Friday at 1845hr the same week. (3mks)

9. Simplify the expression:  $\frac{9t^2 - 25a^2}{6t^2 + 19at + 15a^2}$  (3mks)

10. Use reciprocal and cube root tables to evaluate (3mks)

$$\frac{5}{63.34} - \sqrt[3]{0.0169}$$

11. A Kenya company received US Dollars M. The money was converted into Kenya Shillings in a bank which buys and sells foreign currencies.

	<u>Buying (in Ksh)</u>	<u>Selling (in Ksh)</u>
1 Sterling Pound	125.78	126.64
1 Us Dollar	75.66	75.86

- (a) If the company received Ksh.15, 132,000, calculate the amount, M received in US Dollar. (2mks)

(b) The company exchanged the above Kenya shillings into Sterling pounds to buy a car in Britain. Calculate the cost of the car to the nearest Sterling pound (2mks)

12. A trader sold a dress for Ksh 7200 allowing a discount of 10% on the marked price. If the discount had not been allowed the trader would have made a profit of 25% on the sale of the suit. Calculate the price at which the trader bought the dress. (3mks)

13. Use logarithms tables to evaluate. (4mks)

$$\sqrt[3]{\frac{36.72 \times (0.46)^2}{185.4}}$$

14. A certain two-digit number is equivalent to five times the sum of the digits. It is found to be 9 less than the number formed when the digits are interchanged. **Find** the number. (3mks)

15. A man standing 20m away from the foot of a vertical pole observes the top of the pole at an angle of elevation of  $30^\circ$ . He begins to walk along a straight line on level ground towards the pole. **Calculate** how far he walked before the angle of elevation of the top of the pole becomes  $80^\circ$ . (3mks)

16. Find the acute angle  $y$  if  $\sin 4y = \cos 2y$  (2mks)

**SECTION B (50MKS)**

17. Mambo poured spirit into a test tube which has hemispherical bottom of inner radius 1.5cm. He noted that the spirit is 8cm high.

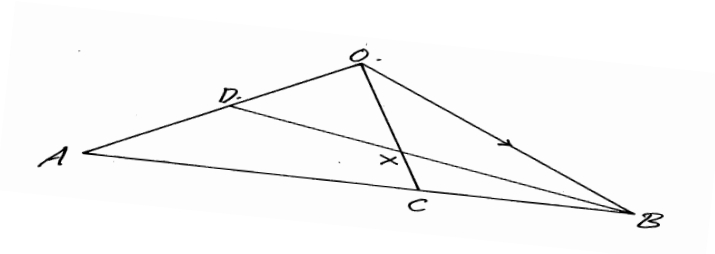
(a) What is the area of surface in contact with spirit? (4mks)

(b) Calculate volume of spirit in the test tube. (4mks)

(c) If Mambo obtained the mass of the spirit as 10g. Calculate the density of the spirit.

(2mks)

18. The figure below C is a point on AB such that  $AC:CB=3:1$  and D is the mid -point of OA. OC and BD intersect at X.



Given that  $\mathbf{OA} = \mathbf{a}$  and  $\mathbf{OB} = \mathbf{b}$

(a) Write the vectors below in terms of  $\mathbf{a}$  and  $\mathbf{b}$ .

(i)  $\mathbf{AB}$  (1mk)

(ii)  $\mathbf{OC}$  (2mks)

(iii)  $\mathbf{BD}$  (1mk)

(b) If  $\mathbf{BX} = h \mathbf{BD}$ , express  $\mathbf{OX}$  in terms of  $\mathbf{a}$ ,  $\mathbf{b}$ , and  $h$ . (1mk)

(c) If  $\mathbf{OX} = k \mathbf{OC}$ , find  $h$  and  $k$ . (4mks)



(d) Hence express  $\mathbf{OX}$  in terms of  $\mathbf{a}$  and  $\mathbf{b}$  only. (1mk)

19. A straight line  $L_1$  has a gradient  $^{-1/2}$  and passes through point P (-1, 3). Another line  $L_2$  passes through the points Q (1, -3) and R (4, 5). Find.

(a) The equation of  $L_1$ . (2mks)

(b) The gradient of  $L_2$ . (1mk)

(c) The equation of  $L_2$ . (2mks)

(d) The equation of a line passing through a point S (0, 5) and is perpendicular to  $L_2$ . (3mks)

(e) The equation of a line through R parallel to  $L_1$ . (2mks)

20. A certain number of people agreed to contribute to buy novels worth sh. 1200. Five of them pulled out and the others agreed to contribute an extra Sh. 10 each. Their contribution brought novels worth sh.200 more than they originally expected.

a) If the original number of people was  $x$ , write an expression of how much each was to contribute. (1mk)

b) Write down two expressions on how much each contributed after the five pulled out and reduced them to a single equation. (2mks)

c) Calculate how many people made the contribution (5mks)

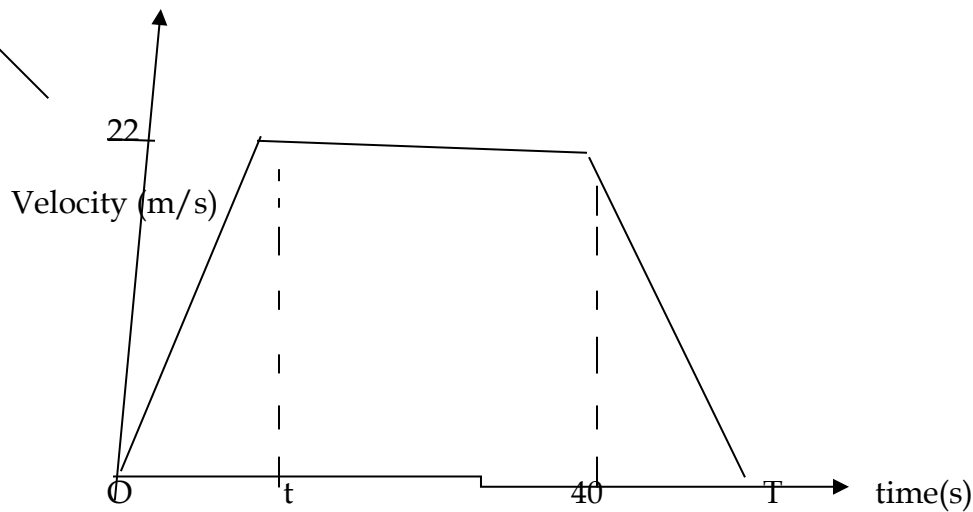
d) How much did each contribute?

(2mks)

21. (a) In 2001 the total cost of manufacturing an article was Sh.1250 and this was divided between the cost of material, labour and transport in the ratio 8: 14: 3. In 2004 the cost of the material was doubled, labour cost increased by 30% and transport costs increased by 20%. Calculate the cost of manufacturing the article in 2004. (6mks)

(b) For the same article in (a) above, the cost of manufacturing in 2005 was sh. 1981 as a result of increase in labour costs only. Find the percentage increase in labour cost of 2004. (4mks)

22. The figure below shows a velocity - time graph of a car journey.



The car starts from rest and accelerates at  $2.75\text{m/s}^2$  for  $t$  seconds until its speed is  $22\text{m/s}$ . It then travels at this velocity until 40 seconds after starting. Its breaks bring it uniformly to rest. The total journey is  $847\text{m}$  long and takes  $T$  seconds.

Calculate the

(i) Value of  $t$  (3mks)

(ii) Distance travelled during the first  $t$  seconds (2mks)

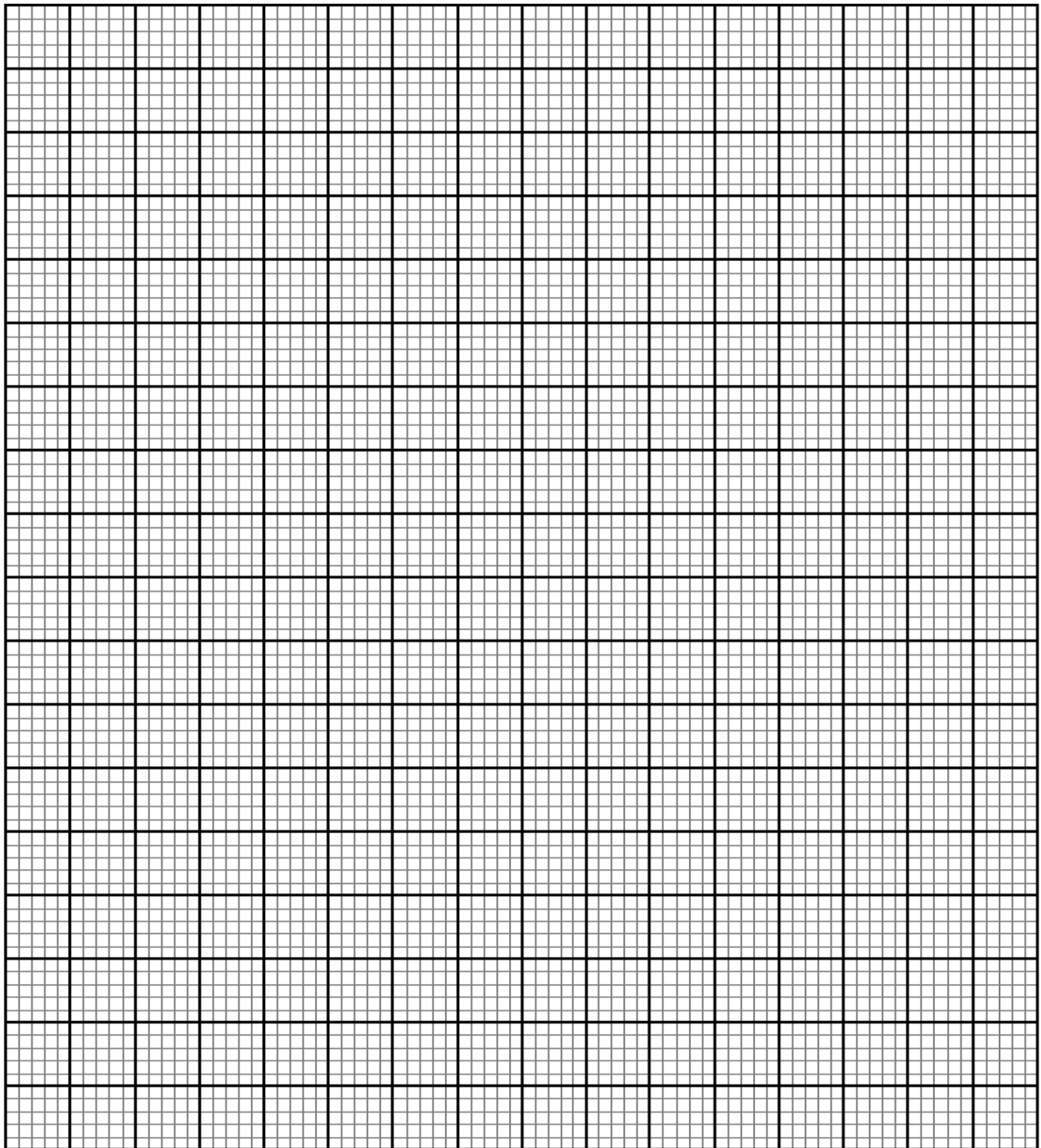
(iii) Value of T (3mks)

(iv) Final deceleration (2mks)

23. A triangle with A(-4, 2), B(-6, 6) and C(-6, 2) is enlarged by a scale factor -1 and centre (-2, 6) to produce triangle A<sup>1</sup>B<sup>1</sup>C<sup>1</sup>.

a) Draw triangle ABC and A<sup>1</sup>B<sup>1</sup>C<sup>1</sup>.and state its coordinates

(4mks)



b) Triangle  $A^1B^1C^1$  is then reflected in the line  $y = x$  to give triangle  $A^{11}B^{11}C^{11}$ . draw  $A^{11}B^{11}C^{11}$ . and state its coordinates 3mks

c) If triangle  $A^{11}B^{11}C^{11}$  is mapped onto  $A^{111}B^{111}C^{111}$  whose co-ordinates are  $A^{111}(0, -2)$ ,  $B^{111}(4, -4)$  and  $C^{111}(0, -4)$  by a rotation. Find the centre and angle of rotation. (3mks)

24. The following are masses of 25 people taken in a clinic.

20	35	29	45	60
66	56	29	48	37
59	64	24	28	32
35	45	48	52	55
54	55	36	39	35

(a) Using a class width of 8 and starting with the lowest mass of the people. Make a frequency distribution table for the data. (3mks)

(b) Calculate the median mass of the people. (3mks)

(c) On the grid provided, draw a histogram to represent the information. (4mks)

